Strand - Measurement and Geometry



.Area

The size of a surface or the amount of space of a flat or two-dimensional shape is called its *area*.

Common units of area are:

square millimetres (mm²) square centimetres (cm²) square metres (m²) hectares square kilometres (km²)

 $1 \,\mathrm{cm}$

The unit used would depend on the size of the area.

 1 mm^2 is the area equal to a square with a side length of 1 mm.

 1 cm^2 is the area equal to a square with a side length of 1 cm.

 1 m^2 is the area equal to a square with a side length of 1 m.

1 hectare is the area equal to a square with a side length of 100 m.

1 km² is the area equal to a square with a side length of 1 km.

This square has an area of 1 cm^2 .

But many shapes would have the same area.

Examples All the shapes below have an area of 4 cm^2 .





Area EXERCISE 12A

- **1.** Each of the small squares in the following shapes is 1 mm². How many mm² are in each shape?
 - (a) (b) (c) (d) (e) (f)
- **2.** Each of the squares in the following shapes is 1 cm². How many cm² are in each shape?



3. How many mm^2 are in one cm^2 ?

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4. Choose the alternative which is the best estimate of the area of each of the following objects.

(a) The display of	f your calculator.		
$\mathbf{A} 1 \text{ mm}^2$	B 10 mm ²	C 10 cm ²	D 100 cm^2
(b) A page of this	book.		
$\mathbf{A} 4 \mathrm{cm}^2$	B 40 cm ²	C 400 cm ²	D 4000 cm ²
(c) A squash cour	t.		
A 50 m^2	B 500 m ²	C 5000 m ²	D 50 000 m ²
(d) New South W	ales		
A 8000 km ²	B 80 000 km ²	C 800 000 km ²	D 8 000 0000 m ²
(e) Your foot prin	t.		
A 16 cm ²	B 160 cm ²	C 1600 cm^2	D 16 000 cm^2

5. State which one of the following pairs of objects has the larger area. (a) A square with side length 10 cm or a circle with diameter 10 cm.



with an area of 2 units.

- (a) Use 8 matches to form a shape with an area of 2 units.
- (b) Use 8 matches to form a shape with an area of 3 units.
- (c) Use 8 matches to form a shape with an area of 4 units.
- (d) Use 10 matches to form a shape with an area of 4 units.
- (e) Use 12 matches to form a shape with an area of 5 units (2 ways).
- (f) Use 12 matches to form a shape with an area of 6 units.
- (g) Use 12 matches to form a shape with an area of 9 units.



Conversions





Convert the following areas to the units shown in the brackets.





EXERCISE 12B

- 1. Change the following areas to the units shown in the brackets.
 - (b) 9 m^2 (a) 5 km^2 (m^{2}) (cm^2) (d) 2.7 km^2 (c) 2 cm^2 (mm^2) (m^2) (e) 5.391 m^2 (cm^2) (f) $0.058 \text{ cm}^2 \text{ (mm}^2)$ (g) 0.0092 m^2 (h) 0.00041 km^2 (m²) (mm^2) (i) 23.8 cm^2 (i) $0.00579 \text{ m}^2 \text{ (mm}^2)$ (mm^2)
- 2. Change the following areas to the units shown in the brackets.
- 3. Change the following areas to the units shown in the brackets.
 - (a) 43 cm^2 (b) 7500 m^2 (mm^2) (km^2) (d) 2.32 cm^2 (c) 8.3 mm^2 (cm^2) (m^{2}) (e) 76 000 mm^2 (cm^2) (f) 5 380 000 m^2 (km^2) (mm^2) (g) 7.2 cm^2 (h) 8.3 m^2 (km^2)
- **4.** (a) The floor area of a room was calculated to be 90 000 cm². Convert this area to m².
 - (b) Which of these units is more convenient? Why?
- 5. (a) The area of a computer screen was calculated to be $60\ 000\ \text{mm}^2$. Convert this area to mm^2 .
 - (b) Which of these units is more convenient? Why?
- **6.** Choose which unit of area would be most convenient to measure the following areas.



- (a) The area of a football ground.
- (b) The area of a paddock on a farm.
- (c) The area of Kakadu National Park.
- (d) The area of a piece of paper.
- (e) The area of a finger nail.
- (f) The floor area of a house.



Using a Grid





EXERCISE 12C

1. Use the 1 cm grid to find the area of the shapes below.



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Example

It is only possible to find an approximate area of a shape with curves when using a grid. Estimate the area of the shape in each square then add all these to find the approximate total area.



2. Use the 1 cm grid to find the approximate area of the shapes below.







Squares and Rectangles

EXERCISE 12D

1. Find the area of each of the following shapes if each small square is 1 cm².



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2. Use the dimensions shown to find the area of each of the following rectangles.



- 3. (a) Find the area of a square with 9 metre sides.(b) Find the area of a 9 cm × 12 cm rectangle.
- **4.** Lin wants to plant lawn in her yard. The dimensions of her yard are 30 metres \times 40 metres.
 - (a) What is the area of Lin's yard?
 - (b) The amount of lawn seed required is 1 kg for every 100 m². How many kilograms of lawn seed will Lin need?
 - (c) Lin's lawn seed grew well.She now has to cut it. Lin's lawn mower has a width of 40 cm.How far will Lin walk if she mows all the lawn in her yard?



- **5.** The perimeter of a paddock is 300 metres. The length of the paddock is 30 metres longer than the width. What is the area of the paddock?
- **6.** (a) List the dimensions (whole numbers only) of all the rectangles that can be formed having perimeters of 16 metres.
 - (b) Find the area of each of these rectangles.
 - (c) What are the dimensions of the rectangle with the largest area?
 - (d) What is the name given to this type of rectangle?
 - (e) Use this information to find the area of the largest rectangle that could be formed having a perimeter of 40 metres.
- **7.** A small area of bush land is in the shape of a rectangle that is 300 metres long and 200 metres wide.

A community group wants to increase the size of the bush land to encourage the native animal and bird life. Each year, for three years, they plant trees and increase the length and width of the bush land by 50 metres.

- (a) What is the area of the bush land before the tree planting began?
- (b) What is the area of the bush land at the end of the first year of tree planting?
- (c) What is the increase in the area of the bush land in the first year?
- (d) By how much did the area of the bush land increase in the three years of tree planting?

Composite Shapes

Find the area of the shaded region in each of the following shapes.





Example 2

The area of the shaded region is equal to the area of the larger rectangle minus the area of the smaller rectangle.

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Area = (14 \times 9) - (6 \times 3)
= 126 - 18
Area = 108 cm<sup>2</sup>
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EXERCISE 12E

Find the area of each of the shaded regions below.





Hectares

EXERCISE 12F



1. Find the area, in hectares, of the following shapes.



- 2. Change the following areas to m².
 (a) 6 hectares (b) 15 hectares (c) 5.75 hectares (d) 0.3 hectares
- **3.** Dulte owned a block of land that was 4 hectares. Find the length of this block of land if it is 100 metres wide.
- **4.** Cameron worked on a cattle farm in Queensland that was 5 km long and 4 km wide. How many hectares is this farm?
- 5. A square property is 1764 hectares. Find the side length of the property.



Triangles

EXERCISE 12G

- 1. Use the 1 cm square grids in each of the following diagrams to:
 - (i) find the area of the rectangle indicated with the dark line.
 - (ii) find the area of the shaded triangle.



2. Is there any relationship between the area of the rectangle and the area of the triangle in each diagram? If there is, state this relationship.



3. Find the area of each of the following triangles.



Parallelograms EXERCISE 12H



Find the area of each of the following parallelograms.





Trapeziums

EXERCISE 12I



Find the area of each of the following trapeziums.





Kites

EXERCISE 12J



1. Find the area of each of the following kites.



2. Shaun wants to make a kite to fly. He found the dimensions of two different kites and these are shown here. What is the area of each of these kites?



- **3.** Jorga found the following plans to make a kite.
 - (a) If Jorga wanted to make a kite that had a width (*w*) of 60 cm, find:
 - (i) the height (h) of the kite.
 - (ii) the area of the kite.
 - (b) If Jorga wanted to make a kite that had a height (*h*) of 1.2 metres, find:
 - (i) the width (*w*) of the kite.
 - (ii) the area of the kite.
- 4. Marlee wanted to make the kite shown here. He wanted to make it without wasting material. Describe how he could make this kite without wasting any material by cutting pieces out from one piece of material.

Show clearly the size of the piece of material.





Rhombuses

A rhombus is a parallelogram that has all four sides of equal length. There are two ways to calculate the area of a rhombus depending on which dimensions are given.

Method 1

If the base length and height are given, the area can be calculated the same way as for a parallelogram.



Method 2

If the length of the diagonals are given, the area can be calculated the same way as for a kite. This is because the diagonals of a rhombus are perpendicular as for a kite.





EXERCISE 12K



Find the area of each of the following rhombuses.





Circles

ACTIVITY

Step 1 Using a compass, or otherwise, draw a circle of known radius on a 1 cm grid.

In the example shown here the circle has a radius of 2 cm.

Step 2 Find an approximate area of the circle by adding all the 1 cm² squares and parts of squares.
Note: estimate the area of the sections that are not complete squares. In this example the approximate area of the circle is:



approximate area = $0.3 + 0.9 + 0.9 + 0.3 + 0.9 + 0.9 + 0.3 + 0.9 + 0.9 + 0.3 + 0.9 + 0.9 + 0.3 + 0.9 + 0.9 + 1 + 1 + 1 + 1 = 12.4 \text{ cm}^2$

Step 3 Copy and complete this table for different radii. The example of R = 2 cm is shown.

R	\mathbf{R}^2	A	$\frac{A}{R^2}$
2	4	12.4	3.1

- **Step 5** What do you notice about the value of $\left(\frac{A}{R^2}\right)$?
- Step 6 What should be the value of $\left(\frac{A}{R^2}\right)$ correct to five decimal places?
- Step 7 What is the symbol given to this?
- *Step 8* Complete these equations using this symbol:





EXERCISE 12L



Find the area of each of the following circles. Give answers to one decimal place.



Problems on Area

EXERCISE 12M

1. Find the area of the shaded regions below.









- **3.** A rhombus has an area of 3200 cm². The height of the rhombus is half the base length. What is the height of the rhombus?
- **4.** A rhombus has an area of 1200 cm². One diagonal is 20 cm longer than the other. Find the lengths of the diagonals.
- 5. The symmetric drawing below is made of a square, two triangles and four rhombuses. The side length of each rhombus is the same as the side length of the square. The area of the square is 1600 cm².
 (a) What is the name given to the type of triangles?
 - (b) What is the area of each of the rhombuses?



- 6. Saffy used mosaic tiles to decorate items of furniture. The mosaic tiles she used were *square* with side length of 20 mm. How many of these tiles would she need to decorate the following items?
 - (a) A drink coaster that was 100 mm square.
 - (b) A rectangular board that was 20 cm long and 10 cm wide.
 - (c) A rectangular coffee table that was 1.5 m long and 50 cm wide.
 - (d) A square piece of artwork that had an area of 1600 cm^2 .
 - (e) A circular table that had a diameter of 80 cm. (Assume she can neatly break the tiles so there is no wasted tiles)
 - (f) A wall in her bedroom that had an area of 6.5 m^2 .

- 7. A piece of wire is in the shape of a circle with radius 10 cm. What length of wire would be needed to form a square that has the same area as the circle? Give answer to one decimal place.
- **8.** A farmer is harvesting all the wheat from his farm. The farm is 64 hectares and is in the shape of a square. He is using a harvester that is 20 metres across and can travel at an average speed of 100 metres per minute.
 - (a) What are the dimensions of the farm?
 - (b) How long would it take the harvester to travel the length of the farm?
 - (c) How many times will the farmer need to drive the harvester the length of the farm to harvest all the wheat?
 - (d) How long will it take to harvest all the wheat?
- **9.** Cheryl is a photographer. She has a photo that is $16 \text{ cm} \times 8 \text{ cm}$ that she

wants to enlarge to be twice as long and twice as wide.

- (a) What is area of the original photo?
- (b) What is the difference between the area of the enlarged photo and the area of the original photo?
- (c) How many copies of the original photo would have the same area as the enlarged photo?
- **10.** Rodney was given the task of painting all the lanes around an athletics field. The dimensions of the field are shown here and there are 8 lanes that are 1 metre wide.
 - (a) What is the area to be painted?

Give answer to the nearest m².

(b) If each litre of paint covers 10 m², how many litres of paint will Rodney need?





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11. A map of South America is shown below. There are 13 countries in South America and these are all coloured and listed alphabetically.



By comparing the sizes of the countries, arrange them in order from the largest to the smallest.

With the countries arranged in the correct order, match the letters next to the countries to spell the answer to this riddle.

What goes putt-putt-putt-putt?



PROBLEM SOLVING

- 1. Xanda owned a *square* block of land that had an area of 4 hectares. He wanted to divide the block into eight equal rectangular blocks to sell.
 - (a) Describe two ways he could divide the land into eight equal rectangular blocks.
 - (b) What would be the dimensions of each small block in each of these two subdivisions?
- Hilda wants to build a pen for her rabbits in the backyard. She buys 12 metres of wire mesh that she is going to use as a border. Hilda decides to use the fence in the backyard as one side of the pen and the wire mesh to make the other three sides of the rectangular pen.





- (a) Guess which values for the length and width would give the largest area of the rabbit pen.
- (b) Copy and complete the table below showing all the possible values for the length and width (use only whole numbers) if all of the wire mesh is used.



Calculate the area for each.

Length (m)	Width (m)	Area (m ²)



PUZZLES

1. Remove 6 matches to leave exactly 2 squares.



- **2.** (a) Rearrange 4 matches to make exactly 3 squares.
 - (b) Rearrange 2 matches to make exactly



- **3.** (a) Form 2 equilateral triangles using 7 matches.
 - (b) Form 4 equilateral triangles using 9 matches.
 - (c) Form 5 equilateral triangles using 9 matches.
 - (d) Form 8 equilateral triangles using 6 matches.
 - (e) Form 4 equilateral triangles using 6 matches.
- **4.** Each of the shapes below are divided into 4 identical parts. Can you divide a *square* into 5 identical parts?_____



5. All sections of this shape are squares. The area of C = 64 cm² The area of D = 81 cm² (a) Find the area of all of the other squares.
(b) Is the total shape a square?





CHAPTER REVIEW

1. Find the areas of the shapes below.



2. Find the area of the shaded regions below.



- 3. Find the area of a 0.5 m \times 0.2 m rectangle giving the answer in: (a) m² (b) cm² (c) mm²
- **4.** A farm is in the shape of a rectangle and is 2.5 km long and 3 km wide. Find the area of the farm in hectares.